

IN THE SPECIFICATION:

Please replace the following paragraphs of the specification as filed:

[0037] From the origin of the isoparametric co-ordinate systems for quadrilateral elements, the new location of node i as shown in Figure 1 can be expressed as

$$P_i' = \frac{1}{N(2 - [[w]])} \sum_{n=1}^N W_n (P_{nj} + P_{nl} - rP_{nk}) \quad (2)$$

where the variational weighting factor and the positional function for each element can be expressed as

$$F_n = \frac{W_n}{N(2 - r)}; \quad \Omega_n = (P_{nj} + P_{nl} - rP_{nk}) \quad (2a)$$

and N is the number of elements connected to node I, i-j-k-l represents an average connected quad, r is the coupling factor between Laplacian and isoparametric methods, P_{nj}, P_{nk}, P_{nl}, represent the position vectors of the j-th, k-th and l-th nodes of the [[n-the]] n-th connected quad respectively, P_i' represents the new location of the node to smooth, and W_n represents weight factors for each connecting element n such that

$$\sum_{n=0}^N W_n = 1.0;$$

[0039] Note that when $r = 0$, equation (1) (2) reduces to Laplace smoothing. When $r = 1.0$, a pure isoparametric grid is produced with quad elements showing very low skewness, but the nodal lines of the mesh become zig-zag. Experience with scheme has proven that $r = 0.5$ results in good quality meshes with an overall skewness that is almost invariably better than the Laplacian variants.

[0048] The governing equation for equipotential (Winslow) smoothing can be written for node i as

$$\alpha P_{i\xi\xi} - 2\beta P_{i\xi\eta} + \gamma P_{i\eta\eta} = 0; \quad (4)$$

where $[[x,h]]_{\xi,\eta}$ are logical variables that are harmonic in nature, while α, β, γ are constant coefficients that depend on the problem.

[0053] where σ is the smoothing operator, $\sigma(P_i)$ indicates $[[,]]$ node i is smoothed, N denotes number of elements connected to node i , θ_{\max} , θ_{\min} are the element allowable angular limits, and α_{ji} denotes the included angle of element j at node i .

[0054] Constrained Movement: Since this smoother is most beneficial to users who are trying to modify existing meshes, add features and build geometry from them, many users would prefer to move nodes in a constrained manner. For example, they may not want their mesh nodes to move off their current location by more than a certain amount. Once the user specifies such a node movement tolerance $dTol$, the nodes are moved from their present location such that they always reside within the sphere of radius $R = dTol$ as shown in Figures 7A and 7B.

[0065] Ability to preserve mapped-meshes: Most smoothing algorithms do not recognize mapped/structured grids. The angle smoother employs a Winslow smoothing algorithm [12] for nodes that are connected to 4 quadrilaterals or 8 triangles. The benefits of the variational smoother are illustrated in Figures 9A-9C. Figure 9A shows a 4X6 mapped mesh on a concave region.